## University of Mumbai

## Examination 2020 under cluster

$\qquad$ (Lead College Short name)
Program: Computer Engineering
Curriculum Scheme: Rev2016
Examination: Second Year
Course Code: CSC303 and
Course Name: Discrete Mathematics
Time: 1 hour
Max. Marks: 50

For the students:- All the Questions are compulsory and carry equal marks .

| Q1. | The relation R is said to be an equivalence relation if it is |
| :---: | :---: |
| Option A: | Reflexive, asymmetric and transitive |
| Option B: | Reflexive, asymmetric |
| Option C: | Reflexive, antisymmetric and transitive |
| Option D: | Reflexive, symmetric and transitive |
| Q2. | If $\mathrm{A}=\{1,2,3\}$ and $\mathrm{R}=\{(1,1),(2,2)\}$ then R is, |
| Option A: | Reflexive and transitive |
| Option B: | Reflexive and symmetric |
| Option C: | Antisymmetric and transitive |
| Option D: | Symmetric but not transitive |
| Q3. | Let $\mathrm{f}(\mathrm{x})=\mathrm{x}+3, \mathrm{~g}(\mathrm{x})=\mathrm{x}-4$ and $\mathrm{h}(\mathrm{x})=2 \mathrm{x}$ find gofoh( x$)$ and $\operatorname{hogof}(\mathrm{x})$. |
| Option A: | $\operatorname{gofoh}(\mathrm{x})=2 \mathrm{x}-1$ and $\operatorname{hogof}(\mathrm{x})=2 \mathrm{x}-2$ |
| Option B: | $\operatorname{gofoh}(\mathrm{x})=2 \mathrm{x}-3$ and $\operatorname{hogof}(\mathrm{x})=2 \mathrm{x}-1$ |
| Option C: | $\operatorname{gofoh}(\mathrm{x})=2 \mathrm{x}+6$ and $\operatorname{hogof}(\mathrm{x})=2 \mathrm{x}-4$ |
| Option D: | $\operatorname{gofoh}(\mathrm{x})=2 \mathrm{x}+3$ and $\operatorname{hogof}(\mathrm{x})=2 \mathrm{x}+6$ |
| Q4. | Which of the following is most appropriate formula to represent statement? "Gold and silver ornaments are precious." <br> The following notations are used. <br> $G(x)$ : $x$ is gold ornament <br> $\mathrm{S}(\mathrm{x})$ : x is silver ornament <br> $\mathrm{P}(\mathrm{x})$ : x is precious |
| Option A: | $\forall x(P(x) \rightarrow(G(x) \wedge S(x))$ ) |
| Option B: | $\forall x(G(x) \wedge(S(x)) \rightarrow P(x)$ |
| Option C: | $\exists x((G)(x) \wedge(S(x)) \rightarrow P(x))$ |
| Option D: | $\forall x((G)(x) \vee(S(x)) \rightarrow P(x)$ |
| Q5. | The complement of 2 in the given lattice is |
| Option A: | 30 |
| Option B: | 5 |
| Option C: | 15 |

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| Option D: | 10 |
| :---: | :---: |
| Q6. | Consider the Hasse diagram shown below, which of these diagrams represents lattice |
| Option A: | i \& iv only |
| Option B: | ii \& iii only |
| Option C: | iii only |
| Option D: | i, iii \& iv only |
| Q7. | What is the correct translation of the following statement into the mathematical logic <br> "some real numbers are rational" |
| Option A: | $\exists \mathrm{x}($ real $(\mathrm{x}) \vee$ rational $(\mathrm{x})$ ) |
| Option B: | $\forall x($ real $(\mathrm{x}) \rightarrow$ rational $(\mathrm{x})$ ) |
| Option C: | $\exists x(\operatorname{real}(\mathrm{x}) \wedge$ rational $(\mathrm{x})$ ) |
| Option D: | $\exists \mathrm{x}($ rational $(\mathrm{x}) \rightarrow$ real $(\mathrm{x})$ ) |
| Q8. | Find the sequence of the following generating function as, $(1+X)^{3}$ |
| Option A: | \{1,3,3,1,0,0,0\} |
| Option B: | \{3,3,3,3,0,0,0\} |
| Option C: | \{1,1,1,1,0,0,0\} |
| Option D: | \{3,1,3,1,3,1,3\} |
| Q9. | With reference to below graphs which statement is true. <br> Graph G1 <br> Graph 62 |
| Option A: | Both graphs are isomorphic |
| Option B: | Graphs are not isomorphic |
| Option C: | Cannot determine |
| Option D: | Graph G1 is subgraph of Graph G2. |
| Q10. | With reference to below graph which statement is true |

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|  | Graph G1 <br> Graph G2 |
| :---: | :---: |
| Option A: | Both graphs are isomorphic |
| Option B: | Graphs are not isomorphic |
| Option C: | Cannot determine |
| Option D: | Graph G1 is subgraph of G2 |
| Q11. | with references to following graph which statement is true |
| Option A: | Graph is Eulerian graph. |
| Option B: | Graph is not a Eulerian graph. |
| Option C: | Not connected graph. |
| Option D: | Bipartite graph |
| Q12. | which of the following statements is/are TRUE for undirected graphs? <br> P: Number of odd degree vertices is even <br> Q: Sum of degrees of all vertices is even |
| Option A: | P only |
| Option B: | Q only |
| Option C: | Both P and Q |
| Option D: | Neither P nor Q |
| Q13. | If 7 colours are used to paint 50 bicycles then at least how many bicycles will be of the same colour. |
| Option A: | 57 |
| Option B: | 10 |
| Option C: | 9 |
| Option D: | 8 |
| Q14. | Consider $\mathrm{A}=\{1,2,3,4,5,6\}$ is a finite Abelian group under multiplication modulo 7. Find the inverse of 5 and 2. |
| Option A: | 3 and 4 respectively |
| Option B: | 4 and 3 respectively |
| Option C: | 3 and 6 respectively |
| Option D: | 2 and 5 respectively |

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| Q15. | Find the hamming distance between X and Y as $\mathbf{X}=\mathbf{1 1 0 1 1 0}$ and $Y=\mathbf{0 0 0 1 0 1}$ |
| :---: | :---: |
| Option A: | 4 |
| Option B: | 3 |
| Option C: | 5 |
| Option D: | 6 |
| Q16. | Let $A$ and $B$ be two sets and let $A^{C}$ and $B^{c}$ denote the complements of the set $A$ and B. The set <br> (A-B) $U(B-A) U(A \cap B)$ is equal to |
| Option A: | A U B |
| Option B: | $\mathrm{A}^{\mathrm{c}} \mathrm{U} \mathrm{B}^{\mathrm{c}}$ |
| Option C: | $\mathrm{A} \cap \mathrm{B}$ |
| Option D: | $\mathrm{A}^{\mathrm{c}} \cap \mathrm{B}^{\mathrm{c}}$ |
| Q17. | Let $\mathrm{A}, \mathrm{B}, \mathrm{C}$ be the non-empty sets and let $\mathrm{X}=(\mathrm{A}-\mathrm{B})-\mathrm{C} \quad$ and $\mathrm{Y}=(\mathrm{A}-\mathrm{C})-(\mathrm{B}-\mathrm{C})$ Which of the following is TRUE? |
| Option A: | $\mathrm{X}=\mathrm{Y}$ |
| Option B: | $\mathrm{X} \subset \mathrm{Y}$ |
| Option C: | $\mathrm{Y} \subset \mathrm{X}$ |
| Option D: | X is not equal to Y |
| Q18. | Which of the following is not necessarily a property of a group? |
| Option A: | Commutativity |
| Option B: | Associativity |
| Option C: | Existence of inverse of every element. |
| Option D: | Existence of identity. |
| Q19. | Four fair coins are tossed simultaneously. The probability that at least one head and at least one tail turn up is |
| Option A: | 1/16 |
| Option B: | 1/8 |
| Option C: | 7/8 |
| Option D: | 15/16 |
| Q20. | If $\mathrm{n}(\mathrm{A})=5, \mathrm{n}(\mathrm{B})=8, \quad$ and $\mathrm{n}(\mathrm{A} \cap \mathrm{B})=3$ then $\mathrm{n}(\mathrm{A} \mathrm{U} \mathrm{B})=$ ? |
| Option A: | 16 |
| Option B: | 5 |
| Option C: | 8 |
| Option D: | 10 |
| Q21. | Find then generating function corresponding to the given sequence as ( $1,1,1,1,1 \ldots \ldots .$. |
| Option A: | 1/(1-x) |
| Option B: | 1/(1+x) |
| Option C: | $\mathrm{x} /(1+\mathrm{x})$ |
| Option D: | $\mathrm{x} /(1-\mathrm{x})$ |
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| Q22. | From the given Hasse diagram find the Join and Meet of $\mathrm{A}=\{12,18\}$ |
| :---: | :---: |
| Option A: | Join is 36 Meet is 2 |
| Option B: | Join is 36 Meet is 3 |
| Option C: | Join is 36 Meet and no meet exists |
| Option D: | Join is 18 Meet is 3 |
| Q23. | Consider the set of positive rational numbers $\mathrm{Q}+$ forms an Abelian group under composition defined by $a * b=a b / 2$ <br> Find the identity element of given structure. |
| Option A: | 2 |
| Option B: | 3 |
| Option C: | 4 |
| Option D: | 6 |
| Q24. | The output of the given logical equivalence is $(\neg \mathrm{P} \wedge(\mathrm{P} \vee \mathrm{Q})) \rightarrow \mathrm{Q}$ |
| Option A: | Tautology |
| Option B: | Contradiction |
| Option C: | Converse |
| Option D: | Inverse |
| Q25. | A box contains 6 white balls and 5 red balls. In how many ways, 4 balls can be drawn from the box if, two balls are to be white and two are red. |
| Option A: | 180 |
| Option B: | 330 |
| Option C: | 150 |
| Option D: | 210 |

